### 

### Semester One Examination, 2020

### Question/Answer booklet

# MATHEMATICS METHODS

**UNIT 1**

## Section Two:

## Calculator-assumed

Your Name

Your Teacher’s Name

## Time allowed for this section

Reading time before commencing work: ten minutes

Working time: one hundred minutes

## Materials required/recommended for this section

***To be provided by the supervisor***

This Question/Answer booklet

Formula sheet (retained from Section One)

***To be provided by the candidate***

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper, and up to three calculators approved for use in this examination

## Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| **Question** | **Marks** | **Max** | **Question** | **Marks** | **Max** |
| **9** |  | **9** | **17** |  | **7** |
| **10** |  | **8** | **18** |  | **11** |
| **11** |  | **5** | **19** |  | **6** |
| **12** |  | **8** | **20** |  | **8** |
| **13** |  | **7** | **21** |  | **6** |
| **14** |  | **10** |  |  |  |
| **15** |  | **5** |  |  |  |
| **16** |  | **10** |  |  |  |

**Structure of this paper**

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Section | Number of questions available | Number of questions to be answered | Working time (minutes) | Marks available | Percentage of examination |
| Section One:  Calculator-free | 8 | 8 | 50 | 50 | 33 |
| Section Two:  Calculator-assumed | 13 | 13 | 100 | 100 | 67 |
|  |  |  |  | **Total** | 100 |

**Instructions to candidates**

1. The rules for the conduct of the Western Australian Certificate of Education ATAR course examinations are detailed in the *Year 12 Information Handbook 2020*. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer booklet.
3. You must be careful to confine your answers to the specific questions asked and to follow any instructions that are specific to a particular question.
4. Additional pages for the use of planning your answer to a question or continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number.
5. **Show all your working clearly.**Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you **do not use pencil**, except in diagrams.
7. The Formula sheet is **not** to be handed in with your Question/Answer booklet.

**See Next Page**

**Section Two: Calculator-assumed (100 Marks)**

This section has **thirteen (13)** questions. Answer **all** questions. Write your answers in the spaces provided.

Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.

● Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.

● Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.

Working time: 100 minutes.

**Question 9 {1.1.23, 1.1.24, 1.1.25} (9 marks)**

1. Circle the diagrams that show functions. (2 marks)

|  |  |
| --- | --- |
| (i) |  |
| (ii) |
| (iii) |
| (iv) |

1. State the domain and range for the following functions. (4 marks)

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
|  | |  | | --- | | **Solution** | | Domain:  Range: | | **Specific behaviours** | | ✓ correct domain  ✓ correct range | |

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
|  | |  | | --- | | **Solution** | | Domain:  Range: | | **Specific behaviours** | | ✓ correct domain  ✓ correct range | |

1. If find (3 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ correct value for  ✓ correct expression for  ✓ correct expression for |

1. -1

**Question 10 {1.3.13, 1.3.15, 1.3.16} (8 marks)**

In a school survey of 207 students in Year 11 and Year 12, it was observed that 77 of the 102 Year 12 students studied Mathematics and the 10 students in Year 11 did not study Mathematics.

If one student is selected at random from those surveyed, determine the probability that

1. they were in Year 11. (1 mark)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ correct probability |

1. they studied Mathematics. (1 mark)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ correct probability |

1. they were in Year 12 or studied Mathematics. (2 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ uses inclusion-exclusion principle  ✓ correct probability |

1. They studied Mathematics given they were in Year 11. (2 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ correct numerator  ✓ correct denominator |

1. Without calculating any further probabilities, is there any indication that studying Mathematics is independent of Year? Justify your answer. (2 marks)

|  |
| --- |
| **Solution** |
| The choice of Mathematics is NOT independent of year.  As  but |
| **Specific behaviours** |
| ✓ states ‘not independent’  ✓ uses the rule P(A│B) = P(A) |

**Question 11 {1.1.3, 1.1.4, 1.1.5} (5 marks)**

Consider the graph shown:

A picture containing object, skiing, man, boat

Description automatically generated

1. Find the gradient of the line PQ. (2 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ uses  ✓ correct gradient |

1. Find the equation of the line RS. (2 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ determines gradient of line RS  ✓ determines equation of line RS |

1. Find the coordinates of point S. (1 mark)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ states the coordinates of S |

**Question 12 {1.1.7, 1.1.10, 1.1.12} (8 marks)**

Use your ClassPad to display parabolas , and whose equations are

1. Write down a feature these three parabolas have in common. (1 mark)

|  |
| --- |
| **Solution** |
| . |
| **Specific behaviours** |
| ✓ states parabolas pass through the origin |

1. Write down the turning point for each parabola and state its nature. (3 marks)

|  |
| --- |
| **Solution** |
| For , maximum turning point (  For , maximum turning point  For , minimum turning point |
| **Specific behaviours** |
| ✓ states maximum turning point and its coordinates for  ✓ states maximum turning point and its coordinates for  ✓ states minimum turning point and its coordinates for |

1. Write down the equation of in turning point form and state the line of symmetry.

(2 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ expresses in turning point form  ✓ states equation for the line of symmetry |

1. If the graph of is translated 2 units in the positive direction of the x axis and 2 units in the negative direction of the y axis, write down the new equation for and state its new line of symmetry.

(2 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ writes equation for after the translations  ✓ states equation for the line of symmetry after the translations |

**Question 13 {1.1.15} (7 marks)**

Sketch the graphs of the following functions. Draw and label the key features, including x- and y-intercepts, vertices, asymptotes (if relevant), showing correct general shape and behaviour.

1. (4 marks)



|  |
| --- |
| **Solution** |
| A picture containing text, game  Description automatically generated |
| **Specific behaviours** |
| ✓ draws and labels horizontal asymptote  ✓ draws and labels vertical asymptote  ✓ Plots and labels x-intercept or &  ✓ correct shape with smooth curves |

1. (3 marks)

|  |
| --- |
| **Solution** |
| A picture containing drawing  Description automatically generated |
| **Specific behaviours** |
| ✓ states at (0, 0)  ✓ plots and labels at least one point on the graph (4, 6), (16, 12)  ✓ correct shape with smooth curve |

**Question 14 {1.1.18} (10 marks)**

1. Sketch the graph of each of the following function, labelling intercepts, point of inflection and showing the shape and behaviour as and .
2. (2 marks)

|  |
| --- |
| **Solution** |
| A picture containing screen, building, game  Description automatically generated |
| **Specific behaviours** |
| ✓ plots and label the point of inflection (0, 0)  ✓ current shape with smooth curve |

1. (3 marks)

|  |
| --- |
| **Solution** |
| A picture containing game  Description automatically generated |
| **Specific behaviours** |
| ✓ plots and labels y-intercept (0, 58)  ✓ plots and labels point of inflection (3, 4)  ✓ plots and labels x-intercept (4.26, 0) |

1. Express cubic function in its factorised form and sketch its graph, labelling all intercepts and using arrows to show its shape and general behaviour as and

(5 marks)

|  |
| --- |
| **Solution** |
| A close up of a mans face  Description automatically generated |
| **Specific behaviours** |
| ✓ writes equation in factorised form  ✓ plots and labels all x-intercepts  ✓ plots and labels the y-intercept  ✓ uses arrows to show behaviour as  ✓ general shape with smooth curve |

**Question 15 {1.1.13} (5 marks)**

An online company that sells onesies has modelled their expected number of daily sales (S) against the average daily temperature (T) in .

Their model has S as inversely proportional to for .

On a 10 day in August they sold 20 onesies.

1. Determine the relationship between S and T. (3 marks)

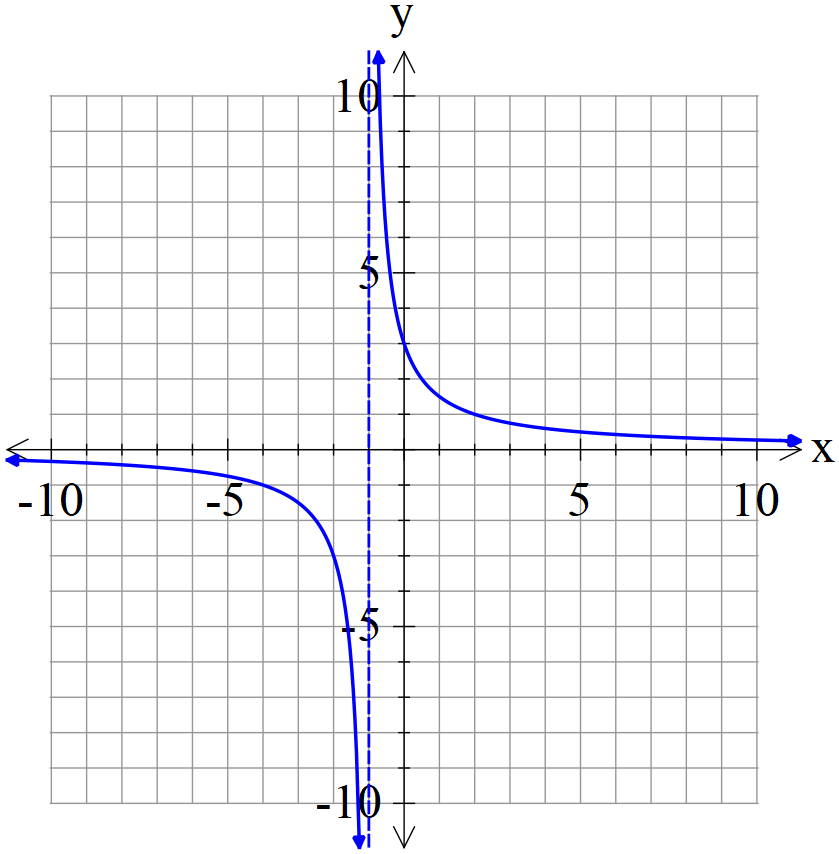
|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ constructs equation for S  ✓ determines k  ✓ determines relationship between S and T |

1. Determine the **number of expected sales** tomorrow if the average forecasted temperature is 29. (2 marks)

|  |
| --- |
| **Solution** |
| Hence, the number of expected sales is 14 |
| **Specific behaviours** |
| ✓ substitutes  ✓ states the number of expected sales as an integer |

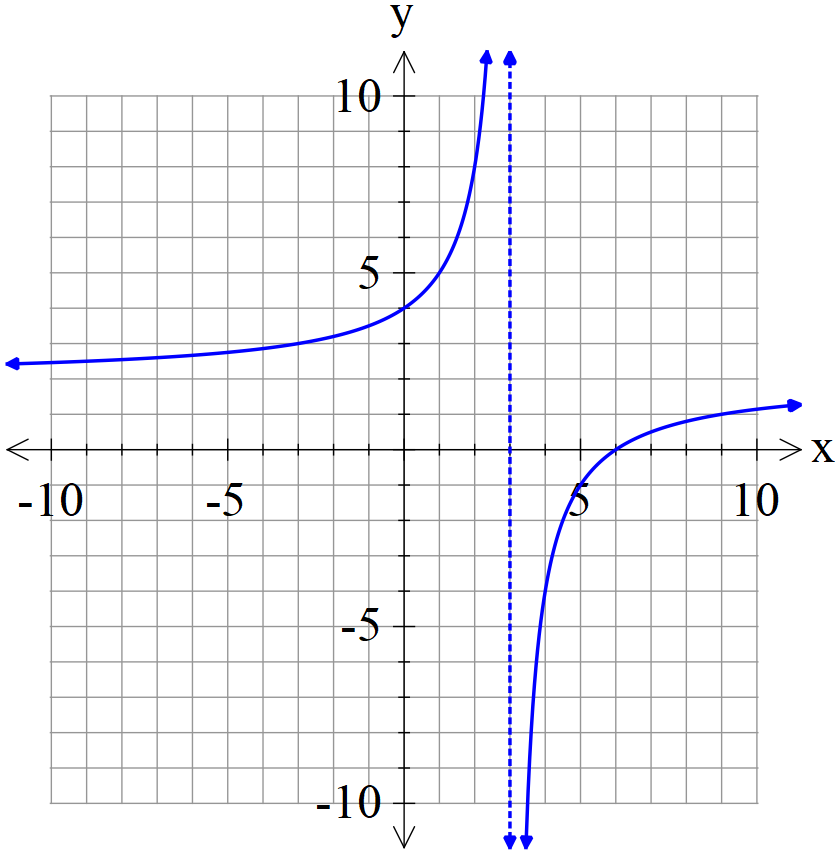
**Question 16 {1.1.14} (10 marks)**

1. State all the asymptotes on each graph below then determine each equation of the rectangular hyperbola:
2. (3 marks)



|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ states asymptotes &  ✓ substitutes point and solves  ✓ states equation |

1. (3 marks)



|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ states asymptotes &  ✓ substitutes point and solves  ✓ states equation |

1. Complete the table below.
2. (4 marks)

|  |
| --- |
| **Solution** |
| |  |  |  |  |  | | --- | --- | --- | --- | --- | | **Curve** | **x-intercept** | **y-intercept** | **Asymptote parallel to the** | | | **x-axis** | **y-axis** | |  |  |  |  |  | |  | None |  |  |  | |
| **Specific behaviours** |
| ✓ correct x-intercepts  ✓ correct y-intercepts  ✓ correct horizontal asymptotes  ✓ correct vertical asymptotes |

**Question 17 {1.1.10} (7 marks)**

A C-9 jet utilised by NASA enters a parabolic flight at an altitude of 9200m to simulate zero gravity. For the duration of the zero-gravity flight, its altitude in metres can be represented as a function of time in seconds as follows:

1. Given that the function passes through the points and , determine the values of , and . (3 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ states value for c  ✓ states value for a  ✓ states value for b |

1. When is the maximum altitude reached by the jet? State the maximum altitude.

(2 marks)

|  |
| --- |
| **Solution** |
| When  Hence, the maximum altitude is 9805m at 11s |
| **Specific behaviours** |
| ✓ correct value for t at maximum altitude  ✓ correct value for A at maximum altitude |

1. Given that the plane exits the parabolic flight at the same altitude it begins at, what is the duration of the zero-gravity simulation? (2 marks)

|  |
| --- |
| **Solution** |
| Hence, the duration is 22s |
| **Specific behaviours** |
| ✓ substitutes A(t) by 9200 and solves for t  ✓ states the duration |

**Question 18 {1.1.26, 1.1.27} (11 marks)**

1. Let
2. What is the equation of the new function if is translated 4 units to the right and 3 units down? What are the coordinates of the point of inflection?

(3 marks)

|  |
| --- |
| **Solution** |
| Point of inflection is |
| **Specific behaviours** |
| ✓ writes equation for  ✓ states point of inflection for |

1. Find the coordinates of the point of inflection of the function .

(2 marks)

|  |
| --- |
| **Solution** |
| Since the point of inflection for is  is the point of inflection for . |
| **Specific behaviours** |
| ✓ correct x value for the point of inflection for  ✓ correct y value for the point of inflection for . |

1. State the sequence of graphical transformation(s) which occurs if:
2. (2 marks)

|  |  |  |
| --- | --- | --- |
| **Solution** | | |
| If in factorised form :  Horizontal dilation by scale factor , then  horizontal translation to the right by 1. | If in expanded form:  Horizontal translation to the right by 2, then  Horizontal dilation by scale factor . | |
| **Specific behaviours** | | |
| ✓ states horizontal dilation in correct order  ✓ states horizontal translation in correct order | | *Incorrect answer if student gives “horizontal*  *dilation by SF ” prior to “translate left by 2”.* |

1. (4 marks)

|  |  |
| --- | --- |
| **Solution** | |
| If in factorised form :  ①Vertical dilation by scale factor  ②Horizontal dilation by scale factor  ③Horizontal translation to the left by  ④Vertical translation down by 1 | If in expanded form  ①Vertical dilation by scale factor  ②Horizontal translation to the left by  ③Horizontal dilation by scale factor  ④Vertical translation down by 1 |
| **Specific behaviours** | |
| ✓ states vertical dilation in correct order  ✓ states horizontal dilation in correct order  ✓ states horizontal translation in correct order  ✓ states vertical translation in correct order | *For both versions, ①&*② *can switch,* ③&④ can  *switch. Incorrect answer if student gives “horizontal*  *dilation by SF ” prior to “translate left by ”.* |

**Question 19 {1.1.26, 1.1.27} (6 marks)**

The graph shows the function .



(a) Sketch the graph of . (3 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ starts at  ✓ passes through  ✓ ends at |

(b) Sketch the graph of . (3 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ starts at  ✓ passes through  ✓ ends at |

**Question 20 {1.3.11, 1.3.12, 1.3.17} (8 marks)**

1000 people were studied to see if they contracted an illness (I) and whether they were vaccinated against it (V). 86 people caught the illness and 348 were vaccinated, including 1 person who caught the illness despite being vaccinated.

1. Given that the above data is representative of a population, find the probability that a person randomly selected from the population:
   * 1. is not vaccinated? (2 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ uses the rule  ✓ correct probability |

* + 1. has caught the illness or is vaccinated? (2 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ uses the rule  ✓ correct probability |

1. Does the vaccination affect a person’s probability of catching the illness? If it does, how is it affected? Justify your answer with calculations. (4 marks)

|  |
| --- |
| **Solution** |
| Yes. It decreases the probability of catching the illness. |
| **Specific behaviours** |
| ✓ states  ✓ states  ✓ states “Yes”  ✓ compares and |

**Question 21 {1.1.20} (6 marks)**

It is found that the shape of a part of a roller coaster ride can be modelled by a cubic function for . The coordinates of several points on the track are (2, 360.5), (6, 195.14), (10, 54.74) and (12, 87.5).

(a) Determine the rule for the function in the form for Find the values of , , and *.*  (4 marks)

|  |
| --- |
| **Solution** |
| OR |
| **Specific behaviours** |
| ✓ correct value for a  ✓ correct value for b  ✓ correct value for c  ✓ correct value for d |

(b) Find the coordinates of the point(s) on the track that is furthest from the ground.

(2 marks)

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ obtains one point and states its coordinates  ✓ obtains two points and states their coordinates |

**END OF QUESTIONS**

Additional working space

Question number:

Additional working space

Question number:

Additional working space

Question number: